



The Concircular Curvature Tensor Of The Locally Conformal Kahler Manifold

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ABSTRACT

In this research, we are calculated components conharmonic curvature tensor in some aspects Hermeation manifold in particular of the Locally Conformal Kahler manifold. And we prove that this tensor possesses the classical symmetry properties of the Riemannian curvature. They also, establish relationships between the components of the tensor in this manifold.

1- Introduction

Concircular curvature tensor is invariant under concircular transformations, i.e. with conformal transformations of space keeping a harmony of functions. The concircular curvature tensor introducer will be Reminded Yano on 1940 as a tensor of type (4, 0) on n-dimensional Riemannian manifold, Conformal transformations of Riemannien structures are the important object of differential geometry, Rawah A.Z. Hassan on 2015 researched concirculac curvature tensor of nearly Kahler manifold, in this paper we investigate the "concircular curvature tensor of locally conformal Kahler manifold".

2- Preliminaries

Let M – "smooth manifold of dimension 2n", the concircular curvature tensor introducer will be Reminded Yano as a tensor of type (4, 0) on n-dimensional Riemannian manifold. An AH -manifold is called a locally conformal Kahler manifold, if foreach point $m \in M$ there exist an open neighborhood U of this point and there exists $f \in C^\infty(M)$ such that $\tilde{U}_f$ is Kahler manifold [2]. We will denoted to the locally conformal Kahler manifold by L.C.K.

Definition 1.1 [2]

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Remark 1.2 [3]

By the Banaru's classification of AH-manifold, the L.C.K- manifold satisfies the following conditions : $B^{abc} = 0$, $B_c^{ab} = \alpha^{[a} \delta_c^{b]}$, where B^{abc} and B_c^{ab} system of function on M.

Theorem 1.3 [4]

The structure equations of L.C.K- manifold in the adjoint G – structure space is given by the following forms :

1. $d\omega^a = \omega_b^a \wedge \omega^b + B_c^{ab} \omega^c \wedge \omega_b$
2. $d\omega_a = -\omega_a^b \wedge \omega_b + B_{ab}^c \omega_c \wedge \omega^b$
3. $d\omega_b^a = \omega_c^a \wedge \omega_b^c + A_{bc}^{ad} \omega^c \wedge \omega_d + \{\frac{1}{2} \alpha^a [c \delta_b^{d]} + \frac{1}{4} \alpha^a \alpha^{[c} \delta_b^{d]}\} \omega_c \wedge \omega_d$

Theorem 1.4 [4]

In the adjoint G – structure spaace, the component of Riemannian curvature tensor of L.C.K- manifold are given by the following forms :

1. $R_{bcd}^a = \alpha_{a[c} \delta_{d]}^b + \frac{1}{2} \alpha_a \alpha_{[c} \delta_{d]}^b$
2. $R_{bcd}^a = -\alpha^{a[c} \delta_{b]}^{d]} - \frac{1}{2} \alpha^a \alpha^{[c} \delta_{b]}^{d]}$
3. $R_{bcd}^a = -2\alpha_{[c}^{[a} \delta_{d]}^{b]}$
4. $R_{bcd}^a = 2\alpha_{[a}^{[c} \delta_{b]}^{d]}$
5. $R_{bcd}^a = A_{bc}^{ad} - \alpha^{[a} \delta_c^{h]} \alpha_{[h} \delta_b^{d]}$

6. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = -A_{\hat{a}\hat{d}}^{\hat{b}\hat{c}} + \alpha^{[\hat{h}]\hat{d}}_{\hat{d}} \alpha_{[\hat{a}]\hat{c}}^{\hat{b}]\hat{h}} \delta_{\hat{h}}^{\hat{c}}$
7. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = A_{\hat{b}\hat{c}}^{\hat{a}\hat{d}} - \alpha^{[\hat{a}]\hat{d}}_{\hat{d}} \alpha_{[\hat{b}]\hat{c}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$
8. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = -A_{\hat{a}\hat{d}}^{\hat{b}\hat{c}} + \alpha^{[\hat{b}]\hat{d}}_{\hat{d}} \alpha_{[\hat{a}]\hat{c}}^{\hat{h}]\hat{b}} \delta_{\hat{h}}^{\hat{c}}$
9. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = \alpha^{[\hat{a}]\hat{c}}_{\hat{c}} \delta_{\hat{b}}^{\hat{d}} + \frac{1}{2} \alpha^{\hat{a}}_{\hat{a}} \alpha^{[\hat{c}]\hat{d}}_{\hat{d}} \delta_{\hat{b}}^{\hat{c}}$
10. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = -\alpha_{[\hat{a}]\hat{c}}^{\hat{b}]\hat{d}} \delta_{\hat{d}}^{\hat{c}} - \frac{1}{2} \alpha_{\hat{a}}^{\hat{b}} \alpha_{[\hat{c}]\hat{d}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$
11. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = -\alpha^{[\hat{a}]\hat{c}]}_{\hat{c}} \delta_{\hat{d}}^{\hat{b}} + \alpha^{[\hat{a}]\hat{d}}_{\hat{d}} \alpha_{[\hat{b}]\hat{c}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$
12. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = \alpha_{[\hat{a}]\hat{c}}^{\hat{b}]\hat{d}} \delta_{\hat{d}}^{\hat{c}} - \alpha_{[\hat{a}]\hat{d}}^{\hat{b}]\hat{c}} \alpha_{[\hat{h}]\hat{c}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$
13. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = -\alpha^{[\hat{a}]\hat{d}]}_{\hat{d}} \delta_{\hat{c}}^{\hat{b}} + \alpha^{[\hat{a}]\hat{b}]}_{\hat{b}} \alpha_{[\hat{h}]\hat{c}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$
14. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = \alpha_{[\hat{a}]\hat{d}}^{\hat{b}]\hat{c}} \delta_{\hat{b}}^{\hat{c}} - \alpha_{[\hat{a}]\hat{b}}^{\hat{b}]\hat{c}} \alpha_{[\hat{h}]\hat{c}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$
15. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = 0$
16. $R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} = 0$

We need the components of Ricci tensor of $L.C.K$ -manifold, so we compute it as the following.

Definition 1.5 [5]

Ricci tensor is tensor of type (2,0) which is defined by $r_{ab} = R_{abc}^c = g^{cd} R_{cabd}$.

Theorem 1.6[6]

In the adjoint G -structure space, the component of Ricci of $L.C.K$ -manifold are given by the following forms:

1. $r_{ab} = \alpha_{[c]b} \delta_c^a + \frac{1}{2} \alpha_c^a \alpha_{[b} \delta_{c]}^a + \alpha_{[c]b]a} \delta_c^a - \alpha_{[c} \delta_{a]}^h \alpha_{[h} \delta_b]^c$
2. $r_{\hat{a}\hat{b}} = -\alpha^{c[b} \delta_a^c] - \frac{1}{2} \alpha^c_a \alpha^{[b} \delta_a^c] - \alpha^{[c]b]}_{\hat{c}} \delta_c^a + \alpha^{[c} \delta_{\hat{h}}^a] \alpha^{[h} \delta_c^b]$
3. $r_{\hat{a}\hat{b}} = 2\alpha_{[c}^{\hat{b}} \delta_{\hat{a}}^c] + A_{\hat{a}\hat{b}}^{\hat{c}\hat{c}} - \alpha^{[c} \delta_{\hat{c}}^h] \alpha_{[\hat{a}]\hat{b}}^{\hat{h}]\hat{c}}$
4. $r_{\hat{a}\hat{b}} = -2\alpha_{[\hat{b}}^{\hat{c}} \delta_{\hat{a}}^c] - A_{\hat{c}\hat{c}}^{\hat{a}\hat{b}} + \alpha^{[\hat{a}]\hat{b}}_{\hat{b}} \alpha_{[\hat{c}]\hat{h}}^{\hat{h}]\hat{a}} \delta_{\hat{h}}^{\hat{c}}$

Remark 1.7 [6]

The value of Riemannian metric g is define by the form

1. $g_{ab} = g_{\hat{a}\hat{b}} = 0$
2. $g_{\hat{a}\hat{b}} = \delta_{\hat{a}}^{\hat{b}}$
3. $g_{a\hat{b}} = \delta_a^{\hat{b}}$

Definition 1.8[5]

Suppose (M, J, g) is a AH -manifold, the cocircular curvature of the $(L.C.K)$ define as tensor $C = \{C_{jkl}^i\}$ of type (3,1) by the form:

$$C_{jkl}^i = R_{jkl}^i - \frac{\chi}{n(n-1)} [r_{il} g_{jk} - r_{ik} g_{jl}]$$

Where R is Riemannian curvature tensor, r is Ricci tensor and g is Riemannian metric and χ scalar curvature.

Theorem 1.9

In the adjoint G -structure space, the components of the cocircular tensor of the $L.C.K$ manifold are given by the following forms:

- 1) $C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} + \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$
- 2) $C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$
- 3) $C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$
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- 5) $C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$
- 6) $C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} + \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$
- 7) $C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$

$$8) C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$$

And the other are conjugate of them.

Proof

1) put $i = \hat{a}, j = \hat{b}, k = \hat{c}, l = \hat{d}$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{\hat{b}\hat{c}} - r_{\hat{a}\hat{c}} g_{\hat{b}\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}}(0) - r_{\hat{a}\hat{c}} g_{\hat{b}\hat{d}}] \quad \text{by}$$

using the remark 1.7

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} + \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$$

2) put $i = \hat{a}, j = \hat{b}, k = c, l = d$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{\hat{b}c} - r_{\hat{a}c} g_{\hat{b}\hat{d}}] \quad \text{If}$$

$c \leftrightarrow d$, then

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{\hat{b}c} - r_{\hat{a}d} g_{\hat{b}\hat{c}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$$

3) put $i = \hat{a}, j = b, k = \hat{c}, l = \hat{d}$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{b\hat{c}} - r_{\hat{a}\hat{c}} g_{b\hat{d}}] \quad \text{If}$$

$\hat{c} \leftrightarrow \hat{d}$, then

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{b\hat{c}} - r_{\hat{a}d} g_{b\hat{c}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$$

4) put $i = \hat{a}, j = \hat{b}, k = \hat{c}, l = \hat{d}$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{\hat{b}\hat{c}} - r_{\hat{a}\hat{c}} g_{\hat{b}\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}}(0) - r_{\hat{a}\hat{c}}(0)]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$$

5) put $i = \hat{a}, j = b, k = \hat{c}, l = d$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{b\hat{c}} - r_{\hat{a}\hat{c}} g_{b\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{b\hat{c}} - r_{\hat{a}\hat{c}}(0)]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$$

6) put $i = \hat{a}, j = b, k = c, l = \hat{d}$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{bc} - r_{\hat{a}c} g_{b\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}}(0) - r_{\hat{a}c} g_{b\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} + \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$$

7) put $i = \hat{a}, j = b, k = c, l = d$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{bc} - r_{\hat{a}c} g_{b\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{1}{n(n-1)} [r_{\hat{a}\hat{d}}(0) - r_{\hat{a}c}(0)]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}$$

8) put $i = \hat{a}, j = \hat{b}, k = c, l = \hat{d}$.

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{\hat{b}c} - r_{\hat{a}c} g_{\hat{b}\hat{d}}]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} [r_{\hat{a}\hat{d}} g_{\hat{b}c} - r_{\hat{a}c}(0)]$$

$$C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK) = R_{\hat{b}\hat{c}\hat{d}}^{\hat{a}} - \frac{\chi}{n(n-1)} (r_{\hat{a}}^{\hat{c}} \delta_{\hat{d}}^{\hat{b}})$$

Proposition 1.10

The cocircular curvature of $(L.C.K)$ manifold satisfies all the properties the algebraic:

$$1) C(LCK)(X_a, X_b, X_c, X_d) = -C(LCK)(X_b, X_a, X_c, X_d)$$

$$2) C(LCK)(X_a, X_b, X_c, X_d) = -C(LCK)(X_a, X_b, X_d, X_c)$$

$$3) C(LCK)(X_a, X_b, X_c, X_d) + C(LCK)(X_b, X_a, X_c, X_d) + C(LCK)(X_c, X_a, X_b, X_d) = 0$$

$$4) C(LCK)(X_a, X_b, X_c, X_d) = -C(LCK)(X_b, X_c, X_a, X_d)$$

Where $X_i \in X(M)$, $i = 1, 2, 3, 4$

proof:

We shall prove just (1) the rest is as proof in the same way

$$1) \quad C(LCK)(X_a, X_b, X_c, X_d) = R(X_a, X_b, X_c, X_d) - \frac{\chi}{n(n-1)} \{g(X_a, X_c)r(X_b, X_d) - g(X_b, X_c)r(X_a, X_d)\} \\ = -R(X_a, X_b, X_c, X_d) + \frac{\chi}{n(n-1)} \{g(X_a, X_c)r(X_b, X_d) - g(X_b, X_c)r(X_a, X_d)\} = -R(X_b, X_a, X_c, X_d)$$

Properties are similarly proved:

$$2) C(LCK)(X_a, X_b, X_c, X_d) = -R(X_a, X_b, X_d, X_c) \\ 3) \quad C(LCK)(X_a, X_b, X_c, X_d) + R(X_b, X_a, X_c, X_d) + R(X_c, X_a, X_b, X_d) = 0 \\ 4) C(LCK)(X_a, X_b, X_c, X_d) = -R(X_c, X_d, X_a, X_b) \\ X_i \in X(M), i = 1, 2, 3, 4$$

(1), (2), (3) and (4) is called an algebra curvature tensor of $(L.C.K)$ manifolds.

The cocircular curvature of $(L.C.K)$ manifolds looks like

$$R(X_a, X_b)X_c = R(X_a, X_b)X_c - \frac{\chi}{n(n-1)} \{< X_b, X_c > X_a r - < X_a, X_c > QX_b\}$$

Where $Q = r$.

By definition of a spectrum tensor.

$$R(X_a, X_b)X_c = R_0 < X_a, X_b > X_c + R_1 < X_a, X_b > X_c + R_2 < X_a, X_b > X_c + R_3 < X_a, X_b > X_c + R_4 < X_a, X_b > X_c + R_5 < X_a, X_b > X_c + R_6 < X_a, X_b > X_c + R_7 < X_a, X_b > X_c$$

Tensor $R_0 < X_a, X_b > X_c$ nonzero – the component have only components of the form:

$$\text{Tensor } C_0(LCK) < X_a, X_b > X_c - \text{components } \{C_0^{a \ bcd}(LCK), C_0^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_1(LCK) < X_a, X_b > X_c - \text{components } \{C_1^{a \ bcd}(LCK), C_1^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_2(LCK) < X_a, X_b > X_c - \text{components } \{C_2^{a \ bcd}(LCK), C_2^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_3(LCK) < X_a, X_b > X_c - \text{components } \{C_3^{a \ bcd}(LCK), C_3^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_4(LCK) < X_a, X_b > X_c - \text{components } \{C_4^{a \ bcd}(LCK), C_4^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_5(LCK) < X_a, X_b > X_c - \text{components } \{C_5^{a \ bcd}(LCK), C_5^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_6(LCK) < X_a, X_b > X_c - \text{components } \{C_6^{a \ bcd}(LCK), C_6^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensor } C_7(LCK) < X_a, X_b > X_c - \text{components } \{C_7^{a \ bcd}(LCK), C_7^{\hat{a} \ \hat{b}\hat{c}\hat{d}}(LCK)\} = \{C_{bcd}^a(LCK), C_{\hat{b}\hat{c}\hat{d}}^{\hat{a}}(LCK)\}$$

$$\text{Tensors } R_0 = R_0 < X_a, X_b > X_c, R_1 = R_1 < X_a, X_b > X_c, \dots, R_7 = R_7 < X_a, X_b > X_c.$$

The basic invariants cocircular $(L.C.K)$ manifold will be named.

Definition 1.11

LCK - manifold for which $C_i(LCK) = 0$ is LCK - manifold of class $C_i(LCK)$, $i = 0, 1, \dots, 7$.

The manifold of class $C_0(LCK)$ characterized by a condition $C_0^{a \ bcd}(LCK) = 0$, or $C^a_{bcd} = 0$, $[C(LCK)(\varepsilon_c, \varepsilon_d)\varepsilon_b]^a \varepsilon_a = 0$. As σ - a projector on $D_f^{\sqrt{-1}}$, that

$$\sigma \circ \{C(LCK)(\sigma X_a, \sigma X_b)\sigma X_c = 0, \\ \text{i.e } (id - \sqrt{-1}J)\{C(LCK)(X - \sqrt{-1}JX, Y - \sqrt{-1}JY)(Z - \sqrt{-1}JZ)\} = 0.$$

Removing the brackets can be received:

$$C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)JX_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)JX_c - JC(LCK)(JX_a, X_b)JX_c + JC(LCK)(JX_a, JX_b)JX_c - \sqrt{-1}\{C(LCK)(X_a, X_b)JX_c + C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)JX_c\} - JC(LCK)(X_a, X_b)X_c - JC(LCK)(X_a, JX_b)JX_c - JC(LCK)(JX_a, X_b)JX_c + JC(LCK)(JX_a, JX_b)JX_c = 0, \\ \text{i.e.1) } C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)JX_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)JX_c - JC(LCK)(JX_a, X_b)JX_c + JC(LCK)(JX_a, JX_b)JX_c = 0,$$

Thus LCK - manifold of class $C_0(LCK)$ characterized by identity

$$2) \quad C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)JX_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)JX_c - JC(LCK)(JX_a, X_b)JX_c - JC(LCK)(JX_a, JX_b)JX_c = 0, X_a, X_b, X_c \in X(M).$$

These equalities are equivalent. The second equality turns out from the first

Replacement Z on JZ .

$$C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)JX_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)JX_c - JC(LCK)(JX_a, X_b)JX_c + JC(LCK)(JX_a, JX_b)JX_c = 0, X_c, X_b, X_c \in X(M).$$

Similarily considering LCK - manifold of classes $R_1 - R_7$ can be received the following theorem.

Theorem 1.12

1) LCK - manifold of class $C_0(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c - C(LCK)(X_c, JX_b)JX_a - C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_c, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c = 0, X_a, X_b, X_c \in X(M).$$

2) LCK - manifold of class $C_1(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)JX_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c = 0, X_a, X_b, X_c \in X(M).$$

3) LCK - manifold of class $C_2(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c + \\ C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)X_c - \\ JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c + \\ JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c = \\ 0, X_a, X_b, X_c \in X(M).$$

4) LCK – manifold of class $C_3(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c + \\ C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)X_c - \\ JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c + \\ JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c = \\ 0, X_a, X_b, X_c \in X(M).$$

5) LCK - manifold of class $C_4(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c + \\ C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)X_c + \\ JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c - \\ JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c = \\ 0, X_a, X_b, X_c \in X(M).$$

6) LCK - manifold of class $C_5(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c + \\ C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)X_c + \\ JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c - \\ JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c = \\ 0, X_a, X_b, X_c \in X(M).$$

7) LCK – manifold of class $C_6(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - \\ C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)X_c + \\ JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c + \\ JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c = \\ 0, X_a, X_b, X_c \in X(M).$$

8) LCK – manifold of class $C_7(LCK)$ characterized by identity

$$C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - \\ C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)X_c + \\ JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c + \\ JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c = \\ 0, X_a, X_b, X_c \in X(M).$$

Definition 1.13

The manifold (M, J, g) refers to as manifold of a class:

1) $\bar{C}_1(LCK)$ if $\langle C(LCK)(X, Y)Z, W \rangle = \langle C(LCK)(X, Y)JZ, JW \rangle$;

2) $\bar{C}_2(LCK)$ if $\langle C(LCK)(X, Y)Z, W \rangle = \langle C(LCK)(JX, JY)Z, W \rangle + \langle C(LCK)(JX, Y)JZ, W \rangle + \langle C(LCK)(JX, Y)Z, JW \rangle$;

3) $\bar{C}_3(LCK)$ if $\langle C(LCK)(X, Y)Z, W \rangle = \langle C(LCK)(JX, JY)JZ, JW \rangle$

Theorem 1.14

Studying and creating some of the relationships involved:

i) $C_0(LCK) = C_3(LCK)$;

ii) $C_1(LCK) = C_2(LCK)$;

iii) $C_4(LCK) = C_7(LCK)$;

iv) $C_5(LCK) = C_6(LCK)$.

Proof: - We shall prove (i)

$$C_0(LCK) = \\ C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - \\ C(LCK)(JX_a, X_b)JX_c \\ - C(LCK)(JX_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c - \\ JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c + \\ JC(LCK)(JX_a, JX_b)JX_c \dots (1)$$

$$C_0(LCK) = \\ C(LCK)(X_a, X_b)X_c - \\ C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c - \\ C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c - \\ C(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)X_c - \\ (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c - \\ (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c - \\ (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c \\ + (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c$$

$$C_0(LCK) = \\ C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c + \\ C(LCK)(JX_a, X_b)JX_c - \\ C(LCK)(JX_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c + \\ JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c + \\ JC(LCK)(JX_a, JX_b)JX_c \dots (2)$$

From (1) and (2) we get

$$C_0(LCK) = \\ C(LCK)(X_a, X_b)X_c - C(LCK)(JX_a, JX_b)X_c - \\ JC(LCK)(X_a, X_b)JX_c + JC(LCK)(JX_a, JX_b)JX_c \dots (3)$$

$$C_3(LCK) = \\ C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c + \\ C(LCK)(JX_a, X_b)JX_c - \\ C(LCK)(JX_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c + \\ JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c + \\ JC(LCK)(JX_a, JX_b)JX_c \dots (4)$$

$$C_3(LCK) = \\ C(LCK)(X_a, X_b)X_c + \\ C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c + \\ C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c - \\ C(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)X_c - \\ (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c + \\ (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c + \\ (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c + \\ (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c$$

$$C_3(LCK) = \\ C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - \\ C(LCK)(JX_a, X_b)JX_c - \\ C(LCK)(JX_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c - \\ JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c + \\ JC(LCK)(JX_a, JX_b)JX_c \dots (5)$$

From (4) and (5) we get

$$C_3(LCK) = C(X_a, X_b)X_c - C(LCK)(JX_a, JX_b)X_c - \\ JC(LCK)(X_a, X_b)JX_c + \\ JC(LCK)(JX_a, JX_b)JX_c \dots (6)$$

From (3) and (6) we get $C_0(LCK) = C_3(LCK)$

Now we shall prove (ii)

$$C_1(LCK) = \\ C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - \\ C(LCK)(JX_a, X_b)JX_c +$$

$$C(LCK)(J X_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (7)$$

$$C_1(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c - C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c + C(LCK)(-\sqrt{-1}J X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c - (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c$$

$$C_1(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c + C(LCK)(J X_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (8)$$

From (7) and (8) we get

$$C_1(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(J X_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(JX_a, JX_b)JX_c \dots (9)$$

$$C_2(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c + C(LCK)(J X_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (10)$$

$$C_2(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c + C(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c + C(LCK)(-\sqrt{-1}J X_a, -\sqrt{-1}JX_b)X_c - (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c - (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c$$

$$C_2(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c + C(LCK)(J X_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (11)$$

From (10) and (11) we get

$$C_2(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(JX_a, JX_b)X_c - JC(LCK)(X_a, X_b)JX_c - JC(LCK)(JX_a, JX_b)JX_c \dots (12)$$

From (9) and (12) we get $C_1(LCK) = C_2(LCK)$

Now we shall prove (iii)

$$C_4(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (13)$$

$$C_4(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c +$$

$$C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c - C(LCK)(-\sqrt{-1}J X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c - (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c$$

$$C_4(LCK) = C(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)JX_c + JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots (14)$$

From (13) and (14) we get

$$C_4(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(J X_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(JX_a, JX_b)JX_c \dots (15)$$

$$C_7(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (16)$$

$$C_7(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c - C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c - C(LCK)(-\sqrt{-1}J X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c + (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c C_7(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c - C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (17)$$

From (16) and (17) we get

$$C_7(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (18)$$

From (15) and (18) we get $C_4(LCK) = C_7(LCK)$

Now we shall prove (iv)

$$C_5(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c + C(LCK)(J X_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (19)$$

$$C_5(LCK) = C(LCK)(X_a, X_b)X_c - C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c + C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c + C(LCK)(-\sqrt{-1}J X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c + (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c - (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c + (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c C_5(LCK) = C(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c +$$

$$C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (20)$$

From (19) and (20) we get

$$C_5(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c + JC(LCK)(JX_a, JX_b)JX_c \dots (21)$$

$$C_6(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(X_a, JX_b)JX_c - C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c - JC(LCK)(X_a, JX_b)X_c + JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (22)$$

$$C_6(LCK) = C(X_a, X_b)X_c + C(LCK)(X_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c - C(LCK)(-\sqrt{-1}JX_a, X_b)(-\sqrt{-1})JX_c + C(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(X_a, X_b)(-\sqrt{-1})JX_c - (-\sqrt{-1})JC(LCK)(X_a, -\sqrt{-1}JX_b)X_c + (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, X_b)X_c + (-\sqrt{-1})JC(LCK)(-\sqrt{-1}JX_a, -\sqrt{-1}JX_b)(-\sqrt{-1})JX_c$$

$$C_6(LCK) = C(X_a, X_b)X_c - C(LCK)(X_a, JX_b)JX_c + C(LCK)(JX_a, X_b)JX_c + C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_c + JC(LCK)(X_a, JX_b)X_c - JC(LCK)(JX_a, X_b)X_c + JC(LCK)(JX_a, JX_b)JX_c \dots \dots \dots (23)$$

From (22) and (23) we get

$$C_6(LCK) = C(LCK)(X_a, X_b)X_c + C(LCK)(JX_a, JX_b)X_c + JC(LCK)(X_a, X_b)JX_b + JC(LCK)(JX_a, JX_b)JX_c \dots (24)$$

From (21) and (24) we get $C_5(LCK) = C_6(LCK)$

Theorem 1.15

Let $S = (J, g = \langle x, x \rangle) -$ is $L.C.K.$ then the following statement are equivalent :

- 1) $S -$ structure of class $\bar{C}_3(LCK)$
- 2) $C_7(LCK) = 0$
- 3) On space of the adjoint $G -$ structure identities $C(LCK)_{bcd}^a = 0$ are fair .

Proof:

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Let $S -$ structure of class $\bar{C}_3(LCK)$. Obviously it is equivalent to identity

$$C(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + JC(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c = 0 ; \varepsilon_a, \varepsilon_b, \varepsilon_c \in X(M). \text{ By definition of a spectrum tensor}$$

$$C(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c = C_0(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_1(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_2(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_3(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_4(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_5(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_6(LCK)(\varepsilon_a, \varepsilon_b)X_c + C_7(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c, \quad \varepsilon_a, \varepsilon_b, \varepsilon_c \in X(M)$$

$$JC(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c = JC_0(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_1(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_2(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_3(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_4(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_5(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_6(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c + JC_7(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c, \quad \varepsilon_a, \varepsilon_b, \varepsilon_c \in X(M)$$

The identity

$$C(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c = 0 \text{ is equivalent to that } C_7(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_4(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_5(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + C_6(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c = 0$$

And this is equivalent to identities $C_7(LCK) = C_4(LCK) = C_5(LCK) = C_6(LCK) = 0$

By virtue of materiality tensor $C(LCK)$ and its properties (3.2.6) received relation which are equivalent to relations $C_7(LCK)_{bcd}^a = 0$, i.e. identity $C_7(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c = 0$

The opposite , according to

$$C(LCK)(\varepsilon_a, \varepsilon_b)\varepsilon_c + JC(LCK)(J\varepsilon_a, J\varepsilon_b)J\varepsilon_c = 0 ; \varepsilon_a, \varepsilon_b, \varepsilon_c \in X(M). \text{ obviously.}$$

Conclusion

The main results of this study are stated below :

- 1) Computing components of this tensor which are $C_0(L.C.K), C_1(L.C.K), C_2(L.C.K), C_3(L.C.K), C_4(L.C.K), C_5(L.C.K), C_6(L.C.K), C_7(L.C.K)$ in Locally Conformal Kahler Manifold $(L.C.K)$.
- 2) Neutral equations for these component $C_0(L.C.K), C_1(L.C.K), C_2(L.C.K), \dots, C_7(L.C.K)$ Almost Hermitian Manifold.
- 3) Find new classes $\bar{C}_0(L.C.K), \bar{C}_1(L.C.K)$ and $\bar{C}_3(L.C.K)$ and proved the structure $\bar{C}_3(L.C.K)$ is $C_7(L.C.K) = 0$, and on space of the adjoint G -structure identities $C(L.C.K)_{bcd}^a = 0$ are fair.

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تنسير الانحناء الدائري في منطوي كوهلر المتطابق محليا

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الملخص

في هذا البحث تم احتساب مركبات تنسير الانحناء الدائري في بعض أصناف المنطوي الهرميتي التقريبي وعلى وجهه الخصوص منطوي كوهلر الكونفورمي المحلي، مع برهنة ان هذا التنزر يمتلك خصائص التناظر الكلاسيكي لتنزر الانحناء الريماني، إضافة الى ايجاد علاقات بين مركبات التنزر في هذا المنطوي.